

## Lab work in photonics Advanced Laser Technologies

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## Advanced laser technologies labworks

This block of practical work will enable you to discover the pulsed lasers used in scientific and industrial contexts. All duration regimes are explored:  $\mu$ s, ns, ps and fs. The wavelengths of the lasers are in the near infrared (typically between 800 nm and 1300 nm) with different laser media (Nd:YAG, Nd:YLF, Nd:YVO4, Ti:sapphire). Non-linear frequency conversions are used to build laser sources in the visible range.

These lasers have been custom-built at the Institut d'Optique to illustrate the operating principles of lasers (Q-switched regime, mode-locked regime). Several experiments are based on industrial lasers resized for teaching purposes.

The set-ups are unique in the world.

At the end of this block of labworks, you will be able to:

- align laser systems (align a laser oscillator by autocollimation, phase-match a non-linear),
- operate complex laser systems (oscillator, amplifier, frequency converters, characterisation systems),
- characterise a pulsed laser in terms of energy and duration,
- make the link between the physical principles of laser sources and technical achievements.

Pre requisite : the knowledge of laser principles is mandatory.

## Construction and characterization of a diode-pumped picosecond laser

The first objective of the labwork is to mount a diode-pumped laser emitting short pulses (of the order of a few picoseconds). The pulses are obtained by passive mode-locking. In a second step, the labwork propose to characterise the pulses temporally.

For the report, answer the questions asked only: the description of the experiment and its alignments are not useful.

**Important note concerning laser safety.** The lasers used is are in class 3R meaning that they are dangerous even with small hazardous reflections.

- Wear the protective sunglasses,
- NEVER look at the beam from the front,
- When taking notes, TURN THE BACK to the LASER,
- Remove any reflective objects.

## I Description of the source

The setup of the laser is shown in Figure 1. The laser uses a wide-stripe laser diode (1 µm by 100 μm) emitting 800 mW at 808 nm at a current of 1 A as a pump source.

The first lens, L<sub>1</sub> (4 mm focal length and 0.5 numerical aperture), collimates the pumping beam. The second lens, L2 (8 mm focal length and 0.5 aperture), focuses it into the laser crystal.

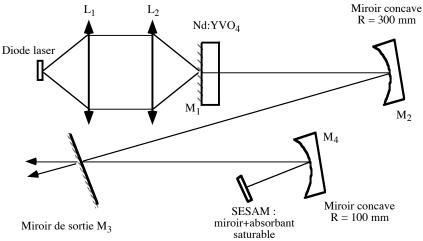


Fig.1: Cavity diagram.

The gain medium is a Nd3+:YVO4 (yttrium vanadate doped with neodymium ion) crystal. Some physical properties are given in table 1. One of the advantages of this crystal is the value of the product "effective cross-section \* fluorescence lifetime" (which characterizes the efficiency of a continuous laser). This product is twice as high as that of Nd:YAG. In addition, Nd<sup>3+</sup>:YVO<sub>4</sub> has a higher absorption coefficient than Nd:YAG (at equal doping), useful for diode pumping with divergent pump beams.

Percentage of Nd ions: 1.1%.

Melting point: 1810°C Density: 4.24 g/cm3

Linewidth at 1064 nm: 1.3 nm

Refractive index at 1064 nm: 1.958 (o) and 2.168 (e)

Fluorescence lifetime: 115 µs

Table 1: Some characteristics of the Nd:YVO4.

The Nd:YVO₄ is a four-level laser described in Figure 2.

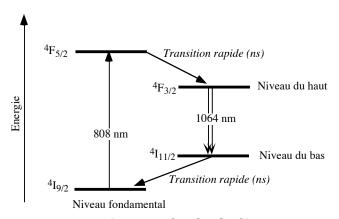


Fig.2: Energy levels of Nd3+.

The crystal used has a length of 2 mm. Its first side has a reflective coating at 1064 nm. It is also anti-reflectively coated at the pump wavelength (808 nm). Its second face is anti-reflective coated at 1064 nm to minimise losses in the cavity. The crystal is prismatic in order to avoid parasitic Fabry-Perot effects between its two faces.

The cavity consists of five mirrors. The first one  $(M_1)$ , is constituted by the first face of the crystal. The second  $(M_2)$ , which is highly reflective at 1.06  $\mu$ m, is a concave mirror with a radius of curvature of 300 mm, which allows a small waist to be obtained in the crystal. The third  $(M_3)$  is the output mirror. Its transmission is 2% at 1064 nm. As it is not placed at the end of the cavity, there are two beams at the output of the laser. The fourth mirror  $(M_4)$  is a concave mirror (R=100 mm) which focuses the beam into the saturable absorber. The fifth mirror, called SESAM (for SEmiconductor Saturable Absorber Mirror) is a Bragg mirror (stack of AlAs-GaAs layers) on which a layer of InGaAs saturable absorber is located.

The latter ensures an absorption of 1% when it is not saturated. It becomes totally transparent when saturated, thus ensuring greater reflectivity for the entire structure. Attention, here, the saturable absorber gives a very low modulation of the losses in the cavity. It cannot therefore be used to favour the Q-switched regime. However, the small loss modulation will favour the mode-locked regime, to the detriment of the continuous regime.

Question to be prepared before arriving in TP: The spectral width of the emission at 1064 nm is given in Table 1 for Nd:YVO4. Assuming that the cavity modes completely fill this spectral band, what is the order of magnitude of the theoretical pulse duration?

Question 1: Explain why and how a saturable absorber with a low modulation amplitude induces mode-locked operation.

Question 2: The distances between the mirrors are as follows (these are orders of magnitude): - distance between M1 and M2: 170 mm

- distance between M2 and M3: around 50 cm
- distance between M3 and M4: around 50 cm
- distance between M4 and SESAM: 55 mm

Draw the beam pattern in the cavity (calculation not necessary), specifying where the waists planes are.

## II Mounting the laser

Mounting the laser source involves two main steps: mounting the Nd:YVO4 laser in continuous operation and then switching to pulse operation by inserting the SESAM into the cavity.

#### II.1 Continuous laser

This part of the labwork is used to adjust the pumping of the amplifying medium and the alignment of the cavity. The aim is to obtain the highest possible output power with a TEM<sub>00</sub> mode of the laser beam. For the adjustments, you have at your disposal an infrared sensitive card, a CCD camera and an infrared viewer.

#### II.1.1 Adjusting the pump optics and the crystal

Place the emitting area of the laser diode at the focus of the first lens and adjust the distance to properly collimate the pump beam in the diffraction-limited direction (vertically).

Before inserting the focusing lens, orient the crystal so that it is autocollimated with respect to the incident beam.

Insert the focusing lens. When the beam from the diode is correctly focused, a whitish dot appears in the crystal. This corresponds to different wavelengths emitted by a process called frequency conversion by energy transfer. In fact, two ions in the upper level (Figure 3) have the ability to interact and exchange their energy in such a way that one of them rises to a higher energy level (4G<sub>7/2</sub>) while the other falls to a lower energy level (4I<sub>13/2</sub>). The ion that has reached the excited state 4G7/2 is radiatively de-excited by emitting red, yellow or green radiation depending on the arrival level. This effect is all the more important as the density of atoms in the upper level is high (the more numerous the ions are in the upper level, the more likely they are to interact). Since this density is a function of the size of the pump beam in the crystal, the more focused the pump beam is, the greater the radiation emitted in the visible.

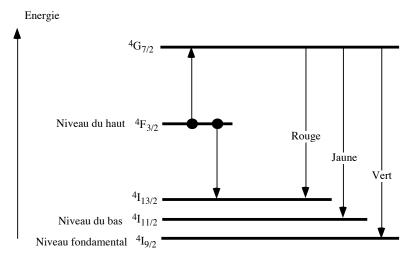


Fig.3: Partial energy diagram of the Nd3+ ion.

## II.1.2 Installation of a first cavity with three mirrors

The first cavity to aligne is described in figure 4. M'<sub>3</sub> is an plane output mirror with a transmission equal to 10 %.

The part of the pump beam transmitted by the crystal will be used to align the cavity. Using a infrared card, place the  $M'_3$  mirror in autocollimation. The laser effect is normally obtained by rotating  $M'_3$  around this position.

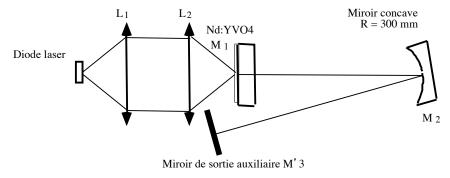


Fig. 4: Diagram of the three-mirror cavity.

Optimising the cavity, mainly by playing with the settings of  $L_1$  and  $L_2$  lenses and the settings of  $M'_3$ , to obtain maximum output power.

**Question 3:** How much power do you get?

#### II.1.3 Installation of the final cavity

Adjust the rest of the cavity by autocollimation using the camera and multiple returns. Remove the auxiliary mirror M'<sub>3</sub>. The laser effect must be achieved.

#### II.2 Pulsed laser

One of the two output beams is sent to a fast photodiode (rise time of the order of 1 ns). This photodiode has a very small surface area, so care must be taken to position it correctly.

**Question 4:** Explain why a fast photodiode must have a small sensitive surface.

Observe the signal on the oscilloscope. The laser should normally produce pulses corresponding to a phase-synchronised regime of the cavity modes (mode-locking).

**Question 5:** What is the repetition rate of the pulses? Deduce the length of the cavity. Is this consistent with the length of the cavity that you can measure with a ruler?

Question 6: Observe the signal on the spectrum analyser. What do the different peaks correspond to?

Question 7: Estimate the rise time of the whole detection chain (photodiode + oscilloscope).

Question 8: Is it possible to correctly observe the temporal shape of the light pulses with the oscilloscope?

## III Temporal characterisation of the pulses

Question 9: Imagining that you take a picture of the pulses coming from the laser (temporal width predicted by the theory), give the spatial extension of the pulses along their propagation axis.

## III.1 Principle

Since the pulses from the laser are too short to be measured with a fast photodiode, indirect time measurement using an optical autocorrelator is required.

The idea is to use frequency doubling in a birefringent KTP crystal. It cut and oriented for phase-matching in type II at 1064 nm: to create a photon at 532 nm, one needs a photon at 1064 nm with ordinary polarization and one at 1064 nm with extraordinary polarization.

The role of the optical autocorrelator is to create two beams of equal intensity I<sub>1</sub> and I<sub>2</sub> at 1064 nm with orthogonal polarisations (ordinary and extraordinary) with an adjustable delay (Fig.5).

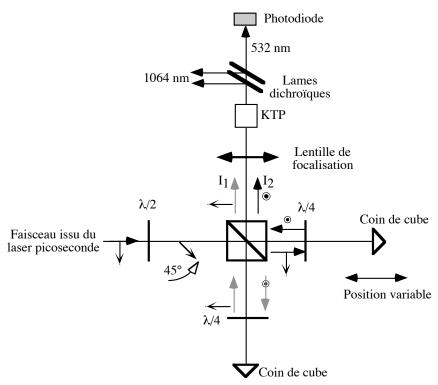


Fig.5: Diagram of the autocorrector.

The two beams are then recombined in the frequency doubling crystal (KTP). The KTP thus sees the intensities  $I_1(t)$  and  $I_2(t-/c)$  where c is the speed of light in air. At instant t, the doubled intensity  $I_{vert}(t)$  is proportional to the product of the intensities on the fundamental beams:

$$I_{vert}(t) I_1(t) * I_2(t-/c).$$

 $I_{\text{vert}}(t)$  varies like the pulses emitted by the laser. However, fast fluctuations cannot be resolved temporally because the detector used here has too slow a response time (typically in the microsecond range). Assuming that the detector has a rectangular pulse response of width  $\tau_r$ , the signal is proportional to the mean value of  $I_{\text{vert}}(t)$ :

$$I_{vert}(\tau_r) = \int_{0}^{\tau_r} I(t)I(t - \delta/c) dt$$

 $\tau_{r}$  being sufficiently long in relation to the characteristic variation times of the intensities, the signal detected in the green corresponds to the autocorrelation function. To access the different values of this function, simply change the delay between the two beams.

The autocorrelator of this labwork looks a bit like a Michelson interferometer, but here it is not an interference phenomenon (the two waves at 1064 nm are perpendicularly polarised).

A first half-wave plate allows the polarisation of the laser to be rotated at 45° to the figure plane. The polarisation beam splitter transmits the polarisation parallel to the figure plane and reflects the perpendicular polarisation. Thus, the half-wave plate and cube are used to create two beams of orthogonal polarization and equal power. Each of the two beams then undergoes a 90° polarisation rotation thanks to a double passage in a quarter-wave plate and a

reflection on a corner cube. Thanks to this rotation, the beam that was transmitted during the first passage through the cube is now reflected during the second passage. Conversely, the other beam is transmitted.

The delay between the two beams can be adjusted by moving one of the two cube corners parallel to the optical axis. The two beams, spatially merged together, are then focused in a KTP crystal.

#### III.2 Settings and measurement

Use the second output beam of the laser.

Approximately equalize the distances of the two channels of the auto-corrector.

Turn the half-wave plate so that the beams are of equal power on both sides of the cube (eye observation with the IR card).

Adjust the quarter-wave plates so that the beams are correctly reflected or transmitted as appropriate.

Adjust the orientation of the corner cubes (WITHOUT FORCING when you reach the translation stop) so that the beams are correctly superimposed after the polarization beam splitter.

Adjust the lens distance-KTP to obtain the most intense green beam possible. CAUTION, the green beam should only be produced when both waves are present simultaneously, check that frequency doubling does not occur when only one of the two beams is present.

Question 10: Knowing that the KTP operates in type II phase matching, explain in which case frequency doubling do occur when only one of the two beams is present? In practice, how can this effect be avoided?

Place the filter that only transmits the beam at 532 nm and a photodiode behind the KTP. The photodiode used here has a response time too long to see the pulsed signal in the green. It therefore delivers a continuous signal whose value is proportional to the average intensity in the green, according to the formula given above.

Measure and plot the intensity in the green according to the delay (which you will vary point by point).

Assuming that the pulses have a Gaussian time profile, the full width at half maximum of the autocorrelation function is related to the pulse duration by the formula:

$$\Delta t_{impulsion} = \frac{\Delta t_{autocorrélation}}{\sqrt{2}}$$

**Question 11:** Evaluate the pulse duration produced by the laser. Comment.

## Optical Parametric Oscillator and Titaniumdoped Sapphire Laser

For the report, only the questions are asked to be answered. Support your answers with diagrams, impulse traces taken with the oscilloscope... Any remark, any further explanation is welcome but there is no need to copy the text of the labwork!

The aim of this labwork is to study two tunable sources from the same pumping laser (Nd:YAG frequency doubled at 532 nm and tripled at 355 nm). The two sources are fundamentally different: the first is based on a non-linear crystal (it is an Optical Parametric Oscillator, OPO). The second is based on a laser crystal, titanium-doped sapphire.

## Very important note on laser safety:

The pump laser you are going to use is dangerous even by diffusion on non-reflective surfaces (class 4). There is also a risk of burning the skin.

- Wearing glasses is absolutely mandatory when the laser is in operation. There are two types of glasses available depending on the wavelengths emitted by the laser.

The green coloured glasses are to be used for the OPO. They protect the eyes from ultraviolet rays. Caution, they do not protect the eyes from the visible beams emitted by the OPO.

The orange-coloured glasses are for use with the titanium-doped sapphire laser. They protect the eyes from the green beam (532 nm) and the beam at 800 nm.

- Remove any reflective object (bracelet, watch, etc.).
- When taking notes, turn your back to the laser,
- The beams are a priori located in a horizontal plane. **Never bend down while the laser is in operation.**
- Do not put your hands in the beams.

## I. Study of a tunable OPO in the visible range

An optical parametric oscillator (OPO) consists of a non-linear crystal placed between two mirrors forming a resonant cavity. The OPO converts a pump beam of wavelength  $\lambda_p$  into two beams called respectively "signal beam", of wavelength  $\lambda_s$ , and "idler beam", of wavelength  $\lambda_i$ . In the OPO we are going to study, only the signal beam oscillates in the cavity.

The general set-up for this study is described in Figure 1 and consists of a flash-pumped, triggered Nd:YAG laser emitting nanosecond pulses of the order of 350 mJ at a frequency of 20 Hz in the near infrared (1064 nm). The radiation is then converted into frequency in two successive non-linear crystals to reach a wavelength of  $\lambda_p$ =355 nm. The first crystal is a frequency doubler converting the infrared beam (1064 nm) into a green beam (at 532 nm, vertically polarised). The second is a crystal called a frequency tripler (3) which performs the

frequency sum between the green beam and the infrared beam which has not been converted to green. The energy per pulse is of the order of 50 mJ at 355 nm. The polarisation of the UV beam is horizontal.

This ultraviolet beam is used to pump the OPO, which consists of a non-linear BBO crystal ( $\beta$ -BaB2O4) and two mirrors reflecting in the visible. The frequency conversion is efficient thanks to type I phase matching: the pump beam is polarised along the extraordinary axis of the crystal while the signal beam and the complementary beam are ordinarily polarised.

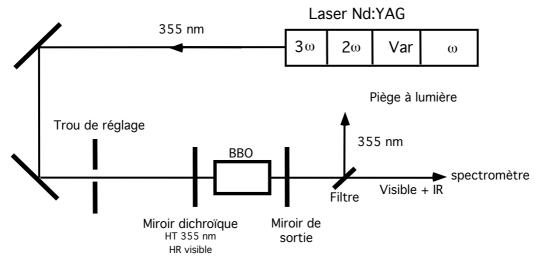


Fig. 1: Experimental setup of the visible OPO

The Nd:YAG source has a power variator (Var) consisting of a half-wave plate and a polarizer before of the frequency converter stages. Two deflecting mirrors allow a good alignment of the UV beam in relation to the rail axis where the OPO is located. A 4 mm diameter hole is used for alignment. The first mirror of the OPO is dichroic, i.e. it transmits the UV beam and completely reflects the visible beams. The second is an output mirror whose transmission curve is given in figure 2.

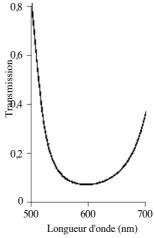


Fig. 2: Transmission of the visible OPO output mirror as a function of wavelength.

At the output of the OPO, a dichroic filter separates the pump wavelength from the emitted wavelengths. It reflects the pump beam that has not been converted in the OPO to a light trap, while it transmits the visible and infrared wavelengths.

**Question 1.1:** Explain why each set of wavelengths (signal + idler) corresponds to a specific phase matching angle of the BBO crystal.

**Question 1.2:** Explain why the rotation of the non-linear crystal will allow the OPO to be tuned.

Adjust the orientations of the phase matching angle of the non linear crystals of the Nd:YAG laser to obtain maximum power in the UV (0.9 - 1 W).

Adjust the alignment of the pump beam with respect to the bench axis at reduced power. Align the pump beam to the bench axis. Then place the crystal in its mount so that its largest dimension is horizontal: the horizontal polarisation of the UV beam is then along the extraordinary axis of the crystal. Place the crystal mount so that the UV beam is centred on the crystal.

Then adjust the mirrors of the OPO and the crystal by autocollimation on the UV beam by superimposing the reflections of the different elements on the alignment hole. The tunability of the OPO is achieved by turning the BBO crystal around a vertical axis. Look for a visible signal by turning the BBO around this axis.

**Question 1.3:** Qualitatively observe the decrease in efficiency of the OPO as the length of its cavity increases. Explain this phenomenon.

**Question 1.4:** Can you tune the OPO by turning the crystal around a horizontal axis? Explain why.

**Question 1.5:** Using the spectrometer, visualise the signal and idler wavelengths. Plot on a graph the wavelengths emitted by the OPO as a function of the angle of rotation of the BBO crystal.

Note 1: As the TP is relatively long, do not take more than ten points.

<u>Note 2</u>: As the crystal mount is not angle-graduated, it is necessary to make a (rough) calibration of the angle of rotation in relation to the adjusting screw on the side of the mount.

**Question 1.6:** What is the wavelength of the beams emitted by the OPO at the degeneracy? Observe the spectrum of the signal and idler beams in the vicinity of the degeneray. How can the observed phenomenon be explained?

**Question 1.7:** Observe the signals from the OPO using the photodiode. What comments can you make?

## II. Study of a titanium-doped sapphire laser

Titanium-doped sapphire crystal has an absorption band in the blue-green and an emission band in the near-infrared, centred at 800 nm. Both absorption and emission are polarisation-dependent. The objective is to study the titanium-doped sapphire laser described in Figure 3.

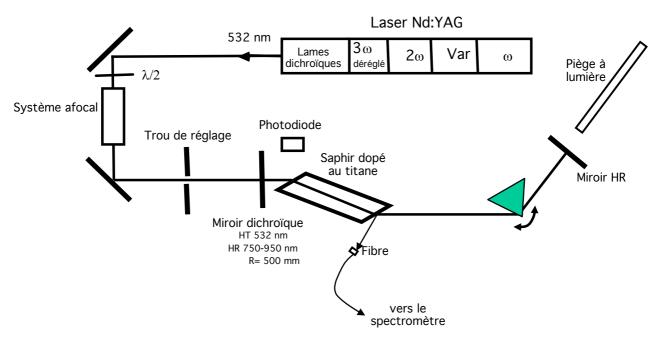


Fig. 3: Experimental set-up for the titanium-doped sapphire laser.

Pumping is performed at 532 nm by the previous Nd:YAG laser, but this time in a frequency doubling configuration (it is necessary to misalign the frequency tripler stage and change the laser output: call the supervisor for this operation).

The pump laser beam at 532 nm is carried to the study bench by means of 2 mirrors reflecting at 532 nm. A half-wave plate is used to control the direction of polarisation of the pump beam. When this is horizontal, the absorption in the titanium-doped sapphire crystal is maximum.

In order to facilitate laser operation, the pump beam size is reduced by means of an afocal system.

The laser cavity consists of two mirrors and a prism. To facilitate the adjustment of the cavity, both mirrors are highly reflective in the infrared. The prism is used to tune the cavity.

The titanium-doped sapphire crystal is cut at Brewster's incidence to limit losses at the interfaces and to avoid additionnal anti-reflective coatings on the faces.

For laser analysis, a photodiode is placed near the laser. This is covered with an orange filter to prevent glare from the pump beam. It will allow the fluorescence of the laser to be observed, as well as the laser effect itself, by diffusion on the optical surfaces.

The spectral analysis will be performed by placing the spectrometer's fibre input close to the crystal, in the path of a laser leakage when the laser is operating.

The green beam that is not absorbed in the titanium-doped sapphire is stopped by means of the light trap.

#### **Question 2.1**: Give a method for adjusting the half-wave plate.

Align the pump beam to the titanium-doped sapphire crystal using the same method as for the OPO setting.

**Question 2.2**: Using the photodiode (with its orange filter), placed on the side of the crystal, observe the fluorescence of the titanium-doped sapphire.

Give a method to measure the lifetime of Ti<sup>3+</sup> ions in the upper level with this experiment. Give the value of the measured lifetime.

Note: By shifting the orange filter slightly, it is possible to bring pump photons to the sensitive surface of the photodiode (the pump diffuses strongly throughout the room). It is interesting to observe both signals at the same time.

#### **Question 2.3**: The prism index is about 1.7 for laser wavelengths.

- Calculate the angle at the top of the prism so that the laser beam is at Brewster's incidence on the entrance and exit faces of the prism.
- What is the angle of incidence so that the prism is at the minimum deviation?

**Question 2.4**: Explain with a figure how the prism can achieve laser wavelength tunability.

Align the prism and the HR mirror. To do this, proceed in two steps: first align these elements with the green beam (adjust the prism around the minimum deviation). Then turn the HR mirror along a vertical axis of rotation to look for the laser effect, which is visible at the signal given by the photodiode.

**Question 2.5**: Observe the laser emission spectrum with the spectrometer. Give the tuning range of the laser.

#### **Question 2.6**: Observe the laser pulse in relation to the pump pulse.

The laser pulse builldup time is defined as the time between the pump pulse and the maximum of the laser pulse. Observe <u>and</u> analyze the evolution of the buildup time as a function of:

- the pump power (variable thanks to the control box),
- cavity losses (by adjusting the HR mirror, the diffraction losses on the laser mode in the cavity can be increased)

**Question 2.7**: Observe the fluorescence of the laser with both the photodiode and the spectrometer. Comment on the evolution of the fluorescence of titanium-doped sapphire with and without laser effect.

## **Question 2.8**: Summary of the labwork

Make a comparison between the two tunable oscillators you have studied in this labwork.

## **L3**

# Second Harmonic Generation in a KDP crystal

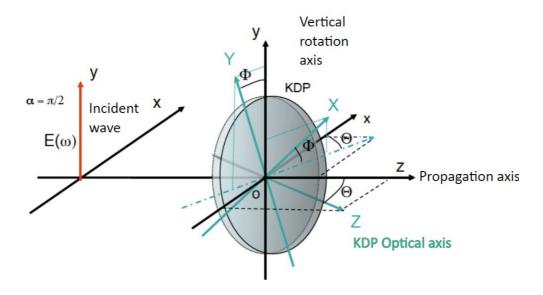
In this session, we study the second harmonic generation process in a non-linear crystal (KDP crystal). We will use a pulsed Nd:YAG @ 1064 nm from laser to produce light @ 532 nm.

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The KDP crystal is a 30 mm diameter, 5 mm thick disk. KDP (KH<sub>2</sub>PO<sub>4</sub>, potassium dihydrogen phosphate) is a birefringent negative uniaxial crystal. It has been cut so its optical axis is perpendicular to the entrance face. This axis is denoted as Oz.

The crystal axes frame is denoted as (X, Y, Z). The lab axes frame denotes as (O, x, y, z). Oz is the propagation direction of the different waves.



**Figure 4.1:** Sketch of the crystal (the crystal is a disk). The crystal axes frame is (OX, Y, Z).  $\Theta$  is the crystal rotation angle around OY (vertical axis of the mount),  $\Phi$  is the rotation angle around OZ (crystal optical axis)

Several mechanical settings allow one to move the crystal:

- The KDP disk can be rotated around the vertical axis (Oy). This will adjust the angle  $\Theta$  between the incident beam (Oz) and the optical axis (OZ). This angle  $\Theta$  is the phase-matching angle.
- It can also be rotated around its own axis OZ to modify the azimuth angle
   Φ.

The Nd: YAG laser is horizontally, linearly polarized. A half wave plate is used to rotate the incident polarization direction on the crystal. The angle a measures the angle between this direction with respect to the vertical axis. In our configuration, the incidence plane will always be defined by Oz and OZ: it is horizontal. The extraordinary direction of polarization is given by the projection of the crystal optical axis (OZ) on the plane wavefront: the extraordinary direction of polarization is then also horizontal. Therefore, the neutral axes will not be affected by a rotation around OZ and a modification of the azimuth angle  $\Phi$ .

The complete setup provides us with an easy access to three degrees of freedom to study SHG:

• the type I and type II phase matching conditions (angle  $\Theta$ )

- the influence of the crystal orientation (angle  $\Phi$ )
- the influence of the pump beam polarization (angle *a*).

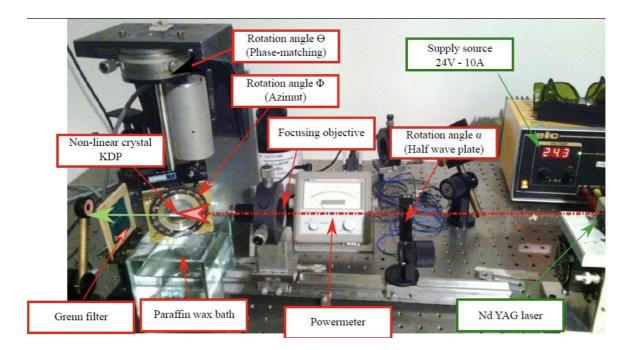


Figure 4.2: Picture of the setup

## 1 Type I phase matching

Two conditions must be fulfilled by a non-linear process: energy conservation and momentum conservation. In the specific case of SHG, the momentum conservation can be written

$$\vec{k}_{2\omega} = \vec{k}_{\omega} + \vec{k}_{\omega}$$

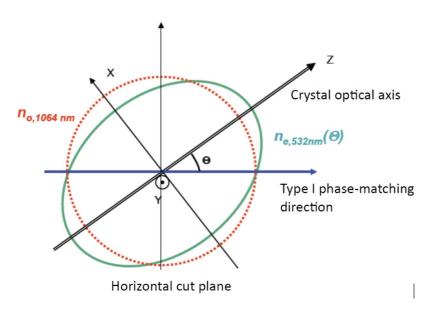
where  $\omega$  is the angular frequency of the fundamental wave and  $2\omega$ , the frequency doubled wave angular frequency. This relation is commonly known as the phase matching condition. For now, we study type I collinear phase matching meaning that both incident fundamental wave vectors are the same.

**Q1:** KDP is a negative uniaxial crystal. Show that the type I phase matching condition can be expressed as:

$$n_{e,2\omega}(\Theta) = n_{o,\omega}$$

where  $n_{e,2\omega}(\Theta)$  is the extraordinary optical index as seen by a frequency doubled wave that propagates with an angle  $\Theta$  with respect to the optical axis.

**Q2:** Use Figure 4.3 to propose a method to determine experimentally the phase matching angle  $\Theta$ .



**Figure 4.3:** Index surfaces in the KDP in the (horizontal) incidence plane. Type I phase-matching

This angle can also be computed from the values of the extraordinary and ordinary indices given by the following Sellmeier equations:

$$n_o^2(\lambda) = 2.25976 + \frac{0.01008956\lambda^2}{\lambda^2 - 0.01294625} + \frac{13.00522\lambda^2}{\lambda^2 - 400}$$
$$n_e^2(\lambda) = 2.132668 + \frac{0.08637494\lambda^2}{\lambda^2 - 0.012281043} + \frac{3.227994\lambda^2}{\lambda^2 - 400}$$

The KDP crystal is a uniaxial negative crystal. We give the following values for the optical indices:

$$n_o(1064) = 1,49384$$
  $n_e(1064) = 1,45985$   $n_o(532) = 1,51242$   $n_e(532) = 1,47041$ 

Use the index surface equation to show that the extraordinary index for a wave propagating with an angle  $\Theta$  can be deduced from the relation:

$$\frac{1}{n_{e,2\omega}^2(\Theta)} = \frac{\sin^2 \Theta}{n_{e,2\omega}^2} + \frac{\cos^2 \Theta}{n_{o,2\omega}^2}$$

**Q3:** Give an expression for the type I phase matching angle  $\Theta_I$  as a function of the ordinary and extraordinary optical index.

## 2 Experimental study of type I phase matching

#### Be careful!

The pump laser emits an invisible IR beam at  $1.064 \, \mu m$ , and its average optical power can be set as high as  $100 \, mW$ . The pulse duration is  $400 \, ps$ , meaning the peak power during the pulses reach  $250 \, kW$ . The repetition rate of the laser can be adjusted between  $0 \, and \, 1 \, kHz$ .

- Always wear safety goggles (type B).
- When not using it, please use the shutter to close the output of the laser.

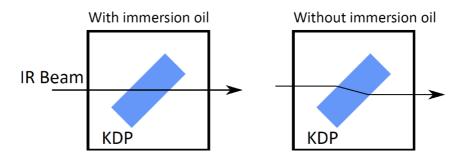
Please manipulate all components with care, including the paraffin wax filled aquarium.

First, switch on the laser.

- First, switch on the laser.
- Switch on the supply at 20 V and 10 A (button on the right)
- Switch on the pulse generator: set the period of the pulses around 14 ms.
- This choice for the period will prevent residual absorption in the paraffin wax and any subsequent thermal effects.
- Switch on the laser itself (On switch on the side, then in front of the system (push twice this last button).
- Open the mechanical shutter (and remember to close it as soon as you do not use the laser).
- Check the output beam with the IR detection card.

#### Paraffin wax bath.

The crystal is immersed in an immersion oil, with an optical index very close from the optical index of the KDP (paraffin wax optical index n = 1, 47). Therefore, the fundamental beam is not deviated when propagating through the interface (see Fig 4.4) The crystal rotation angle around Oy is then directly linked to the angle between the pump beam and the crystal optical axis of the KDP.



**Figure 4.4:** Deviation of the IR beam in the crystal when the KDP crystal is or is not immersed in the paraffin wax bath.

#### **~** Crystal position:

- Set the axes (X, Y) of the crystal at  $\Phi = 45^{\circ}$  with respect to the vertical direction (we will explain later what this configuration is chosen here).
- Move the crystal rotation stage Oy at  $45^{\circ}$  with respect to the normal incidence.
- Move slightly the crystal around this position to observe a green beam. You will probably observe first fringes with the green beam. By adjusting the crystal position, make those fringes disappear. The crystal is then in the correct position.

#### **Q4:** Explain the physical origin of the fringes.

- Now adjust the position of the focusing objective to maximize the green beam intensity.
- Same with the half wave plate orientations
- And finally, same with the angle  $\Phi$
- Check the green beam polarization direction with respect to the axis *Oxyz* with an analyzer and confront this observation to the theoretical predictions.

## **2.1** Experimental measure of the phase matching angle

As seen on figure 4.3, there are two valid directions corresponding to the phase matching angle. Both are symmetric with respect to the optical axis of the crystal.

• You will successively measure those two angular positions to get a better precision on your measurement.

**Q5:** Give an experimental value for the phase matching angle, with its uncertainty, and compare it with the theoretical predictions.

## **2.2** Influence of the azimuth angle $\Phi$

For the KDP in type I phase matching, we can show that the non-linear polarization of interest in our problem can be expressed as:

$$P_x^{NL}(2\omega) = \varepsilon_0 \chi_{eff}^{(2)} E_y^{(2)}(\omega)$$

with  $\chi_{\text{eff}}^{(2)}(2\omega,\omega,\omega) = 2d_{36}\sin(\Theta)\sin(2\Phi)$ 

In the weak depletion regime, the power of the frequency-doubled beam

 $P_{2\omega}$  (expressed in watts) is proportional to:

$$P_{2\omega} = K \left( \chi_{eff}^{(2)} \right)^2 P_{\omega}^2$$

where  $P_{\omega}$  is the power of the fundamental beam (polarized along Oy). K is a proportionality coefficient that is a function of the optical indices, and of other parameters in the experiment (crystal length, waist of the fundamental beam...).

In the previous equation,  $\Theta$  s set by the phase matching conditions. However,  $\Phi$  can still be modified, independently of  $\Theta$ .

• By using a power meter (with a green beam on the path of the beam), measure the optical power @ 532 nm as a function of angle  $\Phi$ . You will have to readjust the angle  $\Theta$  for each position of  $\Phi$ , as the rotation axis of the stage is not exactly the optical axis. You will also have to remove the contribution of the stray light to the measured power. You can extinguish the green beam, either by rotating the incident polarization with the half wave plate, or by matching the condition  $\sin(2\Phi) = 0$ 

• Plot  $P_{2\omega}=f(\Phi)$ .

**Q6:** Comment on the observed behavior.

## **2.3** Influence of the incident polarization

The type I phase-matching conditions are only fulfilled by the component of the field @1064 nm that is ordinary polarized (along the Oy axis of the setup). If the polarization is rotated by an angle a with respect to Oy, one must consider the projection on this axis:

$$E_{v}(\omega) = E_{incident}(\omega) \cdot \cos \alpha$$

The useful part of the fundamental beam power is thus:

$$P_{\omega O_{\rm V}} = P_{\omega} \cos^2 \alpha$$

Use the power-meter to measure  $P_{2\omega}=f(\alpha)$  and plot the corresponding curve.

**Q7:** Comment on the observed behavior.

## 2.4 Angular acceptance

Use the camera to observe the light beam spots on the wall, at the output of the setup. The camera can see radiation @1064 nm, so you can compare both wavelengths' spots.

Be careful and never place the camera directly in the beam!

In presence of a phase mismatch  $\Delta k$ , the optical power of the frequency doubled beam follows a  $sinc^2$  behavior with respect to the phase mismatch

$$rac{P_{2\omega}}{P_{\omega}} \propto P_{\omega} \ell^2 \chi_{eff}^2 \left(rac{\sinrac{\Delta k \ell}{2}}{rac{\Delta k \ell}{2}}
ight)^2$$

**Q8:** Give the expression of  $\Delta k$  as a function of the refractive indices in the case where we are close to the type I phase matching condition (i.e. for  $\Theta \sim \Theta_{\rm I}$ ).

**Q9:** Explain the slight ellipsoidal shape of the frequency doubled beam spot.

~ Evaluate the divergence of the green beam along its smaller dimension by measuring the lateral size of the beam along its propagation direction with a screen (sheet of paper).

**Q10:** Deduce an estimation of the angular acceptance and compare to the theoretical value: 3, 7 mrad. cm.

## 3 Type II phase matching

## **3.1** Theoretical study

For type II phase matching, the momentum conservation can be expressed as:

$$\vec{k}_{2\omega} = \vec{k}_{\omega}^{o} + \vec{k}_{\omega}^{e}$$

The two fundamental photons have orthogonal polarizations.

- **Q11** Explain how to achieve type II phase matching with one single linearly polarized fundamental laser.
- **Q12** The KDP is a negative uniaxial crystal, show that the type II phase match- ing condition is given by:

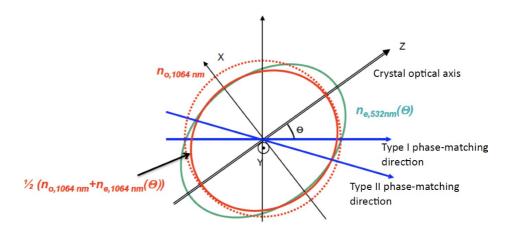
$$n_{e,2\omega}(\Theta) = \frac{1}{2} [n_{o,\omega} + n_{e,\omega}(\Theta)]$$

You could use the same method as previously to get angle  $\Theta$ . Do not do it again during the session. We get a theoretical value:  $\Theta_{II} = 59^{\circ}$ .

We now turn our attention back to the sensitivity of second-harmonic generation to the case of a slight deviation  $\Delta k$  to the phase matching condition.

**Q13:** Using the same analysis as in the previous section, give the expression of  $\Delta k$  as a function of the refractive indices when close to the type II phase-matching condition ( $\Theta \sim \Theta_{II}$ ).

**Q14:** Use figure 4.5 to show that the angular acceptance is better in type II phase-matching than with type I phase-matching.



**Figure 4.5:** Index surfaces in the KDP in the (horizontal) incidence plane. Type II phase-matching compared to type I phase-matching.

## 4 Experimental study of Type II phase matching

To find the type II phase matching condition, the fundamental polarization should ideally be oriented at 45° with respect to the neutral axis of the crystal.

**Q15** By which angle do you have to rotate the half wave plate between the optimal configuration for type I phase matching and type II phase matching?

~ Compare the shape of the green output beam for type II phase matching to the previously obtained shape for type I phase-matching.

## **Q16** Explain the differences.

 Use an analyzer to give the polarization direction of the output beam with respect to the Oxyz axes.

## **Q17** Compare this result to your theoretical predictions.

## **4.1** Phase matching angle measurement

Use the same method as for type I phase matching and give an experimental measure of the type II phase-matching angle with its associated uncertainty.

**Q18** Check if this result is valid according to your theoretical predictions.

## **4.2** Influence of the azimuth angle $\Phi$ .

For type II phase-matching, we can show (see Appendix) that the non-linear polarization of interest can be expressed as:

$$P_x^{ML}(2\omega) = \varepsilon_0 (d_{14} + d_{36}) E_x(\omega) E_y(\omega) \sin(2\Theta) \cos(2\Phi)$$

 $\sim$  Use the power meter to measure the optical power of the frequency doubled beam as a function of the angle  $\Phi$ . Plot this power  $P_{2\omega}$  as a function of  $\Phi$ .

**Q19:** Comment your observations. Superimpose both plots for type I and type II phase-matching to comment on the differences between both situations.

## **4.3** Influence of the incident polarization

a is the angle between the fundamental laser polarization direction and the reference Oy direction.

 $\sim$  Use the power meter and plot  $P_{2\omega}=f(\alpha)$ .

**Q20** Comment and superimpose both plots for type I and type II phase-matching to comment on the differences between both situations.

## **4.4** Comparing the powers for type I and type II phasematching.

**Q21:** Give the maximal output power for the green beams for both type I and type II phase-matching. Comment on the differences predicted by the theoretical considerations in the appendices (you can use the ratio of output optical powers between type I and type II phase-matching).

## Appendix 1: Type I non-linearity

The observed non-linear process is related to a second order induced non-linear polarization. In order to understand more precisely the influence of angles  $\theta_I$ ,  $\alpha$  et  $\Phi$  on this non-linear polarization, one needs to study the second order non-linear susceptibility tensor,  $\chi^{(2)}$ .

We recall that the induces linear polarization can be written as:

$$\vec{P}(\omega) = \varepsilon_0 \chi^{(1)}(\omega) \vec{E}(\omega)$$

For high power densities, second order, third order and higher order terms can add to the linear polarization term. For second harmonic generation, the term is related to the second order non-linear polarization :

$$P_i^{NL}(2\omega) = \varepsilon_0 \sum_{i,k} \chi_{i,j,k}^{(2)} E_j(\omega) E_k(\omega)$$

where i,j,k correspond to the crystal axes X,Y,Z.

The second order non-linear susceptibility, is a tensor of rank 3 with 3^3=27 components. For low absorption regimes and far from resonances, the tensor can be simplified with only 18 components remaining.

Moreover, when the Kleinman symmetry condition is fulfilled, (or for the specific case of SHG), the second order susceptibility tensor can be reduced to a contracted expression, by using the  $d_{ii}$  coefficients:

$$d_{ijk} = \frac{1}{2} \chi_{ijk}^{(2)} = d_{il}$$

The last two indices can be reduced to one single index using the following rule:

Axes du cristal	XX	YY	ZZ	YZ ou ZY	XY ou YX	XY ou YX
jk	11	22	33	23 ou 32	13 ou 31	12 ou 21
l	1	2	3	4	5	6

The tensor can then be expressed as a 6x3 matrix, containing 18 elements:

$$d_{il} = \begin{bmatrix} d_{11} & d_{12} & d_{13} & d_{14} & d_{15} & d_{16} \\ d_{21} & d_{22} & d_{23} & d_{24} & d_{25} & d_{26} \\ d_{31} & d_{32} & d_{33} & d_{34} & d_{35} & d_{36} \end{bmatrix}$$

The KDP crystal under study in this labwork session belongs to the tetragonal symmetry group  $\overline{4}2m$ ,. The contracted susceptibility tensor has only 3 non-zero elements remaining :

$$d_{il} = \begin{bmatrix} 0 & 0 & 0 & d_{14} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{25} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{36} \end{bmatrix}$$

With  $d_{14} = d_{25}$ , and  $d_{14} = 0.39$  pm.V<sup>-1</sup> and  $d_{36} = 0.43$  pm.V<sup>-1</sup>

In the crystal axis frame (O, X, Y, Z):

$$P_i^{NL}(2\omega) = \varepsilon_0 \sum_{j,k} \chi_{i,j,k}^{(2)} E_j(\omega) E_k(\omega)$$

Is given by:

$$\begin{pmatrix} P_X(2\omega) \\ P_Y(2\omega) \\ P_Z(2\omega) \end{pmatrix} = 2\epsilon_0 \begin{pmatrix} 0 & 0 & 0 & d_{14} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{14} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{36} \end{pmatrix} \begin{pmatrix} E_X^2(\omega) \\ E_Y^2(\omega) \\ E_Z^2(\omega) \\ 2E_Y(\omega)E_Z(\omega) \\ 2E_X(\omega)E_Z(\omega) \\ 2E_Y(\omega)E_Y(\omega) \end{pmatrix}$$

so: 
$$P_i^{NL}(2\omega) = \varepsilon_0 \sum_{i,k} \chi_{i,j,k}^{(2)} E_j(\omega) E_k(\omega)$$

$$\begin{pmatrix} P_X(2\omega) \\ P_Y(2\omega) \\ P_Z(2\omega) \end{pmatrix} = 4\epsilon_0 \begin{pmatrix} d_{14}E_Y(\omega)E_Z(\omega) \\ d_{14}E_X(\omega)E_Z(\omega) \\ d_{36}E_X(\omega)E_Y(\omega) \end{pmatrix}$$

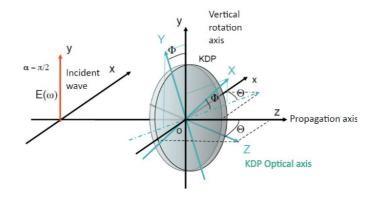
Fo a type I phase-matching in KDP, the incident wave is necessarily ordinary polarized, meaning its projection on the optical axis OZ is zero. There is only one term contributing to the frequency doubled beam:

$$P_Z^{NL}(2\omega) = \varepsilon_0 \chi_{Z,X,Y}^{(2)} E_X(\omega) E_Y(\omega) + \varepsilon_0 \chi_{Z,Y,X}^{(2)} E_X(\omega) E_Y(\omega)$$

$$P_Z^{NL}(2\omega) = 2\varepsilon_0 \chi_{Z,X,Y}^{(2)} E_X(\omega) E_Y(\omega) = 4\varepsilon_0 d_{3\epsilon} E_X(\omega) E_Y(\omega)$$

Moreover, In this configuration, the output beam is extraordinary polarized. The induced non-linear polarization must then be projected onto the direction (Ox).

## Appendix 2: Type II non-linearity



In the crystal axes frame (O,X,Y,Z), the non-linear polarization writes:

$$P_i^{NL}(2\omega) = \varepsilon_0 \sum_{j,k} \chi_{i,j,k}^{(2)} E_j(\omega) E_k(\omega)$$

So:

$$\begin{pmatrix} P_X(2\omega) \\ P_Y(2\omega) \\ P_Z(2\omega) \end{pmatrix} = 2\epsilon_0 \begin{pmatrix} 0 & 0 & 0 & d_{14} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{14} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{36} \end{pmatrix} \begin{pmatrix} E_X^2(\omega) \\ E_Y^2(\omega) \\ E_Z^2(\omega) \\ 2E_Y(\omega)E_Z(\omega) \\ 2E_X(\omega)E_Z(\omega) \\ 2E_X(\omega)E_Y(\omega) \end{pmatrix}$$

$$\begin{pmatrix} P_{X}(2w) \\ P_{Y}(2w) \\ P_{Z}(2w) \end{pmatrix} = 4\varepsilon_{0} \begin{pmatrix} d_{14}E_{Y}(w)E_{Z}(w) \\ d_{14}E_{X}(w)E_{Z}(w) \\ d_{36}E_{X}(w)E_{Y}(w) \end{pmatrix}$$

In type II phase-matching, the incident wave has two components: the ordinary component along (Oy) and the extraordinary component along (Ox). The output beam is an extraordinary wave (polarized along Ox). First, one has to write the components of the incident wave in the crystal axes frame, and then project the polarization on the Ox direction.

 $E_x, E_y, E_z$  can be writen as functions of de  $E_y, E_y, E_z$ :

$$\begin{split} E_{X} &= E_{x} \cos(\Theta) \cos(\Phi) + E_{y} \sin(\Phi) + E_{z} \cos(\Phi) \sin(\Theta) \\ E_{Y} &= -E_{x} \cos(\Theta) \sin(\Phi) + E_{y} \cos(\Phi) - E_{z} \sin(\Phi) \sin(\Theta) \\ E_{Z} &= -E_{x} \sin(\Theta) + E_{z} \cos(\Theta) \end{split}$$

$$E_z = 0$$
 then:

$$E_x = E_x \cos(\Theta)\cos(\Phi) + E_y \sin(\Phi)$$
  

$$E_y = -E_x \cos(\Theta)\sin(\Phi) + E_y \cos(\Phi)$$
  

$$E_Z = -E_x \sin(\Theta)$$

$$\begin{pmatrix} P_{X}(2w) \\ P_{Y}(2w) \\ P_{Z}(2w) \end{pmatrix} = 4\varepsilon_{0} \begin{pmatrix} d_{14}E_{Y}(w)E_{Z}(w) \\ d_{14}E_{X}(w)E_{Z}(w) \\ d_{36}E_{X}(w)E_{Y}(w) \end{pmatrix}$$

$$= 2\varepsilon_{0} \begin{pmatrix} d_{14}E_{x}E_{x}\sin(2\Theta)\sin(\Phi) - d_{14}E_{x}E_{y}\sin(\Theta)\cos(\Phi) \\ -d_{14}E_{x}E_{x}\sin(2\Theta)\cos(\Phi) - d_{14}E_{x}E_{y}\sin(\Theta)\sin(\Phi) \\ -d_{36}E_{x}E_{x}\cos^{2}(\Theta)\sin(2\Phi) + d_{36}E_{y}E_{y}\sin(2\Phi) + d_{36}E_{x}E_{y}\cos(\Theta)\cos(2\Phi) \end{pmatrix}$$

We know that Ex is an ordinary wave and Ey is an extraordinary wave, so the terms ExEx = EyEy do not contribute efficiently to the SHG process for a type II phase-matching. The remaining contributions are:

$$\begin{pmatrix} P_{X}(2w) \\ P_{Y}(2w) \\ P_{Z}(2w) \end{pmatrix} = 4\varepsilon_{0} \begin{pmatrix} d_{14}E_{Y}(w)E_{Z}(w) \\ d_{14}E_{X}(w)E_{Z}(w) \\ d_{36}E_{X}(w)E_{Y}(w) \end{pmatrix} = 2\varepsilon_{0} \begin{pmatrix} -d_{14}E_{X}E_{y}\sin(\Theta)\cos(\Phi) \\ -d_{14}E_{X}E_{y}\sin(\Theta)\sin(\Phi) \\ d_{36}E_{X}E_{y}\cos(\Theta)\cos(2\Phi) \end{pmatrix}$$

Finally, one has to project those components onto the direction Ox.

$$P_x = P_X \cos(\Theta) \cos(\Phi) - P_Y \cos(\Theta) \sin(\Phi) - P_Z \sin(\Theta)$$

We get: 
$$P_{\nu}(2\omega) = \varepsilon_0 (d_{14} + d_{36}) E_{\nu}(\omega) E_{\nu}(\omega) \sin(2\Theta) \cos(2\Phi)$$

# Femtosecond Laser

## 1. Preliminary study: operation of a femtosecond laser

A femtosecond laser is a laser whose modes are phase-locked to produce very short pulses, of about ten to a hundred 10-15 second duration.

The laser studied in thislabwork uses as amplifying medium a titanium-doped sapphire crystal whose emission band extends from 750 nm to more than 900 nm, with a maximum around 800 nm.

Short pulses are synonymous with wide spectral bands. Indeed, for a so-called Fourier transform limited pulse, there is a relationship between the temporal width  $\Delta t$  (at half height) and the spectral width  $\Delta v$  (at half height) of the pulses:

 $\Delta t \Delta v \ge K$  where K is a constant depending on the shape of the pulses. K = 0.44 for a Gaussian time-form pulse and K = 0.315 for an pulse of temporal form in hyperbolic square secant.

There are several techniques for locking modes in phase: active (use of acousto or electro-optical modulators) or passive (use of non-linear effects such as absorption saturation or the Kerr effect). In this labwork, the laser uses a lens created by the Kerr effect in the titanium-doped sapphire crystal. The method is called "Kerr lens mode locking". It provides the shortest pulses.

## 1.1 Principle of the Kerr lens mode lock

The Kerr effect is a non-linear effect which results in the modification of the index of the medium seen by a wave propagating in it according to its intensity I. It is an effect linked to the third order dielectric susceptibility coefficient of  $\chi^3$  the medium. Thus, by noting  $n_0$  the linear index of the medium and  $n_2$  its non-linear index, a beam of intensity I propagate in the medium with the refractive index:

$$n(I) = n_0 + n_2 I$$

In a cavity, the spatial distribution of beam intensity is Gaussian in a plane transverse to the propagation axis. Consequently, when a Gaussian beam of power  $P_0$  passes through a medium with a Kerr effect  $n_2 > 0$ , it is focused (called self-focusing) because the medium acts as a converging Gaussian lens. It is shown that the resulting Kerr lens has a vergence of:

$$D_{Kerr} = \frac{1}{f_{Kerr}} = \frac{n_2 L_{mat}}{\pi w_0^4} P_0$$

where  $w_0$  is the radius of the waist,  $L_{mat}$  is the length of the material passed through and the  $P_0$  peak power of the beam.

For sapphire, the coefficient n<sub>2</sub> is of the order of 3.10<sup>-16</sup> cm<sup>2</sup>/W.

The existence of the Kerr lens will allow us to favour the pulsed regime by introducing more losses on the continuous regime. Indeed, the intensity in the continuous regime is 4 orders of magnitude lower than the intensity in the pulsed regime. Thus, the Kerr lens only exists in the pulsed mode. By inserting a slit in the cavity at a point where the "pulsed" beam is smaller than in the continuous regim, it is then possible to introduce more losses on the continuous beam (see Figure 1).

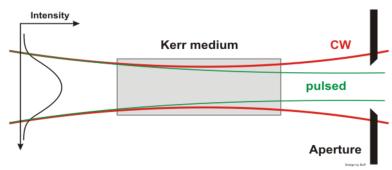


Figure 1: Selection of the pulsed mode by Kerr effect.

### 1.2 Phase dispersion and self-modulation

This part helps to understand how the pulsed regime favoured by the Kerr lens can be stabilised over time.

In the cavity, two phenomena tend to modify the pulse (on the temporal and spectral level). For more details, see Appendix 1.

- The first is the spectral dispersion of the components (in the classic case of a higher index in blue than in red, this is called positive dispersion). Since the spectrum of the pulses from 100 fs to 800 nm is wide (of the order of several nm), the spectral components will propagate at different speeds, each accumulating a different phase. The pulse will tend to widen temporally as it passes through the cavity optics. With each round trip through the cavity, the pulse will accumulate group velocity dispersion (GVD). The "red" part of the pulse will be ahead of the "blue" part of the pulse. This is called frequency drift (or chirp).
- The second is self-phase-modulation. The instantaneous intensity of the pulse varies very strongly over time. This will lead to an instantaneous change in index by the Kerr effect, and therefore to a variation in phase. This Kerr effect observed in the time domain (and not in the spatial domain as in the previous section) is called self-phase-modulation (or SPM). It results in the generation of new frequencies (because frequency is the derivative of temporal phase, see Appendix 1). The new frequencies are time-dependent, resulting in frequency drift. This is of the same type as the frequency drift imposed by dispersion: the "red" part of the pulse will be ahead of the "blue" part of the pulse.

To achieve a stable state of the laser, an optical system must be introduced into the cavity to compensate for this positive dispersion. In this labwork, the system used is a pair of prisms, shown below:

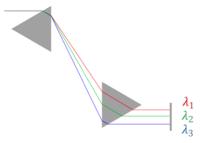


Figure 2: Two-prism system allowing the introduction of negative dispersion for dispersion compensation.

In this configuration, the "red" wavelength  $\lambda_1$  travels a smaller optical path than that of the "blue" wavelength  $\lambda_3$ . An adjustable negative dispersion can therefore be introduced by changing the distance between the prisms or the thickness of glass passed through.

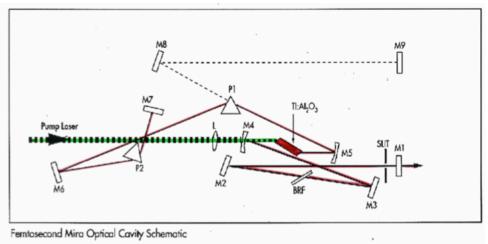
When the prisms are correctly adjusted, it is possible to fully compensate for the positive dispersion created by the cavity components and self-phase-modulation. The laser generally reaches a stable regime called soliton regime (described in Appendix 2) where the pulse retrieved its temporal shape after a round trip in the cavity.

## 1.3 Description of the laser cavity

The crystal is pumped using a frequency-doubled *Nd*: *YAG* laser that emits at a wavelength of 532 nm with a maximum output power of 10 W in continuous operation.

The femtosecond laser cavity is given in Figure 3 (a picture of the laser is given in Appendix 4).

The Lyot filter (birefringent filter, BRF in figure 3) allows the laser to be tuned in wavelength.



## Preliminary questions

**P1**: The length of the laser cavity is about 2 m (linear cavity). Give the pulse rate.

**P2**: The pulse duration will be around 100 fs. Give an order of magnitude of the width of the spectrum emitted by the laser (in nanometres).

**P3**: The average power of the laser will be around 100 mW. Give an order of magnitude of the peak power of each pulse.

**P4**: Calculate an order of magnitude of the focal length  $\mathbf{f}_{\text{Kerr}}$  of the Kerr lens in the titanium-doped sapphire crystal (inside the cavity) where:  $w_0 = 30 \, \mu \text{m}$ ,  $L_{\text{mat}} = 20 \, \text{mm}$ , output mirror transmission: 1%, average laser power: 100 mW, cavity length: 2 m.

**P5** Summarise in a table the optical elements and physical phenomena required to generate femtosecond pulses via Kerr lens mode-locking (some elements may have multiple roles).

Cavity component	Physical effect	Role
Crystal Ti :sapphire	Laser gain	Optical amplifier
Crystal Ti :sapphire	Spatial Kerr effect	
Slot	•••	
Prisms		

## 2. Obtaining the femtosecond regime and first characterizations

LASER SAFETY: the laser is dangerous. Its power makes it necessary to wear type B glasses as soon as the shutter of the pump laser is open.

#### Procedure for obtaining the femtosecond regim

- 1. Open the shutter of the pump laser ("shutter" button).
- 2. Open the slit as wide as possible.
- 3. Adjust the Lyot filter (using the spectrometer) to set the center wavelength of the laser emission towards the center wavelength of the laser.  $800 \text{ nm} \pm 5 \text{ nm}$ .
- 4. If necessary, adjust the back-cavity mirror (M7 in Figure 3) to maximize the output power, the value of which is given in tree units on the laser control box.
- 5. Close the slit to divide the laser power by 2, making sure that the slit is well centred on the beam (the power should be maximized by centering).
- 7. Switch to ML (mode-locking) on the control box. This mode allows the laser to be

- started in femtosecond mode. Indeed, a vibrating optical component (starter mechanism on the photo in appendix 4) will create disturbances in the cavity to obtain noise peaks which will constitute the seed of the pulses.
- 8. The femtosecond regime is obtained when the pulse train is stable and the spectrum is smooth (corresponding to the Fourier transform of a pulse). If the pulse regime is not stable, finely move the Lyot filter over the range [780 nm; 810 nm].

To characterise the femtosecond laser beam, the set-up includes a fast photodiode and oscilloscope as well as a spectrometer.

- **Q1**: Measuring the pulse rate. Deduce the length of the cavity.
- **Q2**: Measure the width of a pulse at half height with the oscilloscope. What do we deduce from this?
- **Q3**: Using the spectrometer, measure the width of the resulting spectral band. From this, deduce the theoretical value of the pulse duration, in the case of a pulse limited by the Fourier transform whose temporal form is a hybrid secant squared.
- **Q4:** Measure the average power of the pulses. Deduce the energy and peak power of the pulses.

# 3 Pulse duration measurement by autocorrelation

## 3.1 Principle of autocorrelation

Since the pulses from the laser are too short to be measured with a photodiode, an indirect measurement of the duration must be made using an optical autocorrelator (Fig.4).

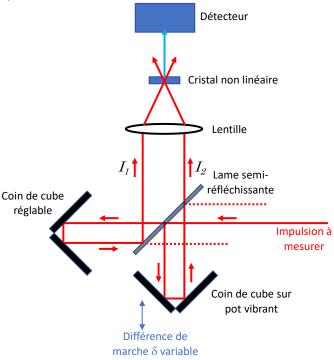


Figure 4: Schematic diagram of an autocorrector.

The idea is to use frequency doubling in a non-linear crystal  $(\chi^2)$ , here a barium beta-borate crystal: BBO). A phase tuning is carried out in order to obtain an efficient frequency doubling: to create one photon at 400 nm, two photons are needed at 800 nm.

The role of the optical autocorrelator is to create two beams of equivalent (ideally equal) intensities  $I_1$  and  $I_2$  (here thanks to a semi-reflecting plate) from the pulse beam to be measured. A movable cube corner allows an adjustable  $\delta$  delay between the two beams.

The two beams are then recombined in the frequency doubling crystal (BBO), located at the focus of a lens. The BBO therefore sees the intensities  $I_1(t)$  and  $I_2(t-\delta/c)$  where c is the speed of light in air. At instant t, the doubled intensity  $I_{blue}(t)$  is proportional to the product of the intensities on the fundamental beams:

$$I_{blue}(t) \propto I_1(t) * I_2(t - \frac{\delta}{\epsilon})$$

I<sub>blue</sub>(t) varies with the pulse rate of the laser, but this intensity cannot be resolved temporally because the detector used here has a too slow response time

(typically in the microsecond range). Assuming that the detector has a rectangular pulse response of width  $\tau_r$ , the signal is therefore proportional to the average value of  $I_{blue}(t)$ :

$$1/\tau_r \int_{0}^{\tau_r} I_1(t) * I_2(t - \frac{\delta}{c}) dt$$

 $\tau_r$  being sufficiently long in relation to the time variations of the intensities, the signal detected in the blue corresponds to the autocorrelation function because  $I_l$  and  $I_2$  come from the same temporal signal. To access the different values of this function, simply modify the delay  $\delta$  between the two beams.

**Q4:** In fig.4, the frequency-doubled beam is the bisector between the two infrared beams: explain why.

### 3.2 Description of the autocorrector

The autocorrelator is described in Figure 5. The first cube corner is mounted on a vibrating pot. The second is mounted on a micrometric translation plate.

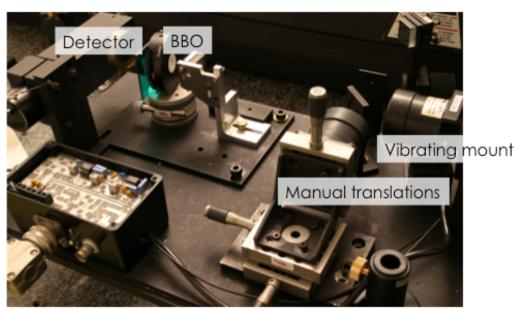


Figure 5: Photo of the autocorrelator.

The signal is detected by a photomultiplier (PM) in front of which a blue filter is placed.

Two external devices are required to use the auto-correlation unit: the vibrating pot power supply, which enables the amplitude and frequency of its movement to be managed, and the PM interface box. These two units will then be connected to the oscilloscope in order to display the autocorrelation signal and the control voltage of the vibrating pot as a function of time.

**Q6**: The BBO crystal is 200 µm thick. Why is it so thin?

**Q7**: The pot vibrates with an amplitude of about 1 mm. Is it suitable for viewing the entire autocorrelation function of a 100 fs pulse?

## 3.3 Adjusting the autocorrector (if necessary)

In order to facilitate the adjustment of the auto-correlation unit, first work with collinear and merged  $I_1$  and  $I_2$  beams on the BBO crystal as shown in figure 6. This setting simplifies the obtaining of the frequency-doubled signal.

The adjustment of the autocorrelation starts with an alignment of the beam to be measured in the centre of the inlet diaphragm and the BBO. To do this, perform a "laser alignment" using the two mirrors at the input of the autocorrelator and remove the focusing length in front of the BBO crystal.

Check that the PM is well centred on the beam (it can easily translate into its mechanical support).

Add the lens on the beam axis, without misaligning the beam.

Switch on the vibratory pot and trigger the oscilloscope on the control signal of the vibratory pot (sinusoidal signal). The vibratory frequency will be set to 20 Hz (at higher frequencies the signal will be attenuated by the response time of the PM and its electronics, which react like a low-pass filter).

Observe a signal doubled in frequency with the PM by playing on the orientation of the BBO.

Adjust the orientation of the BBO and the focus of the lens to have a maximum frequency doubled signal.

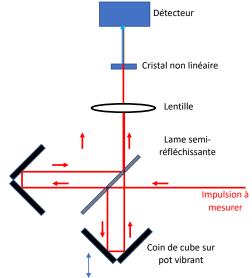


Figure 6: Autocorrelation set with collinear beams.

Shift the lens and the adjustable cube corner to find the configuration shown in Figure 4. Find the autocorrelation function on the oscilloscope.

### 3.4 Measuring pulse duration

The duration of the autocorrelation function is measured by calibration. The adjustable cube wedge is used for this purpose, the translation of which along the beam axis is marked by a micrometer. This micrometer will be used to calibrate the displacement of the vibrating cube corner in order to know the delay it imposes on beam 2. From this, the calibration on the oscilloscope can be deduced.

**Q8:** Translate the cube wedge by noting its displacement (cube wedge vernier reading) for two positions of the autocorrelation function observed on the oscilloscope. The translation of the cube wedge corresponds to an optical delay (by dividing by the speed of light - beware of the factor of 2 related to the return of the beam in the cube wedge). Deduce the calibration of the oscilloscope with respect to the optical delay measured.

**Q9**: It is assumed that the pulse has the form of a hyperbolic secant squared. In this case, the mid-height widths of the pulse  $\Delta t$  and its autocorrelation function  $\Delta t_{\rm autoco}$  are related by  $\Delta t = \Delta t_{\rm autoco}/1.54$  (for information, in the case of a Gaussian form  $\Delta t = \Delta t_{\rm autoco}/\sqrt{2}$ ). Measure the pulse duration and determine the measurement uncertainty.

## 4 Temporal manipulation of femtosecond pulses

Now that you have mastered the femtosecond pulse duration measurement tool, the aim of this part is to make duration measurements under different conditions.

## 4.1 Effect of dispersion in the laser cavity

#### Dispersion and role of prisms in the cavity

In the case of the Ti:Sapphire laser oscillator, self-phase-modulation (SPM) is located in the Ti:Sapphire crystal; group velocity dispersion (GVD) is related to the optical components of the cavity (positive dispersion) and the two-prism negative dispersion system. It is possible to establish a relationship between the duration  $\Delta t$ , dispersion  $\beta_2$ , self-phase-modulation and the electric field envelope |a| (known as the soliton area formula, see Appendix 2):

$$\Delta t = \frac{-\beta_2}{\gamma |a|^2} = \frac{-\phi_{2,cavit\acute{e}}}{\gamma L_{cristal} |a|^2}$$

It can be shown that by changing the dispersion, the regime can remain solitonic. The pulses adapt their duration to find a new balance between dispersion and self-phase-modulation and their spectral phase remains flat. To test this phenomenon, one of the prisms is translated perpendicularly to the optical axis, which has the effect of modifying the thickness of the glass through which it passes, e and thus the second-order spectral phase of the cavity (see Appendix 2).

Vary the amount of material passed through one of the prisms (typically between the 5 and 10 graduations of the vernier).

**Q10**: Plot the duration of the measured pulse as a function of the prism movement. Display the error bars. Do the results validate the soliton air formula?

#### 4.2 Effect of an optical dispersive element on a femtosecond pulse

In a dispersive element, the different spectral components will not travel at the same speed, resulting in a temporal spread of the pulse. This time spread depends on the duration of the input pulse (see Appendix 3).

Place the two crystals of YVO<sub>4</sub> in the beam path.

**Q11**: Measure the pulse duration  $\Delta t_{out}$  using the autocorrelator by varying the duration of the  $\Delta t_{in}$  input pulse (as in 4.1). Make a curve  $\Delta t_{out} = f(\Delta t_{in})$ .

**Q12**: Derive an estimate of the dispersion  $\beta_2$  in  $fs^2.mm^{-1}$  for the YVO<sub>4</sub>.

#### 5 Annexes

## 5.1 Appendix 1 - Phase dispersion and self-phase-modulation

The emitted pulses can be described either in the time domain or in the spectral domain.

We define E(t) the complex amplitude of the associated electric field and E( $\omega$ ) the complex amplitude in the spectral domain, I(t) and I( $\omega$ ) the intensities in the temporal and spectral domains, ( $\omega = 2\pi v$ , v being the frequency considered).

E(t) and  $E(\omega)$  can be written:

$$E(t) = \sqrt{I(t)}.e^{j\varphi(t)}$$
 et  $E(\omega) = \sqrt{I(\omega)}.e^{j\varphi(\omega)}$ 

with  $\varphi(t)$ , the temporal phase of the pulse and  $\varphi(\omega)$ , the spectral phase of the pulse.

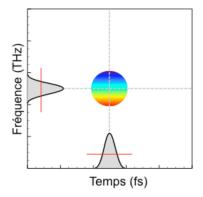
In general (it is the case in this labwork), the two complex amplitudes are linked by the Fourier transform.

#### Group velocity dispersion changes the spectral phase

Usual optical media such as those forming the cavity have a so-called normal or positive dispersion. This has the effect of temporally spreading polychromatic pulses because "red" wavelengths have a higher group velocity than "blue" wavelengths.

To understand the effect of group velocity dispersion, a time-frequency representation called a spectrogram is used. Figure A1.1 (left) shows the typical spectrogram of a femtosecond pulse. In red, the spectral and temporal phases are represented: in the ideal case, they are constant. On the right, the spectrogram of an pulse which has passed through a positive dispersive medium is shown. It can be seen that the pulse is temporally broadened. Its spectrum is identical but its spectral phase is modified.

Red propagates faster than blue: a frequency drift (or chirp) is observed.



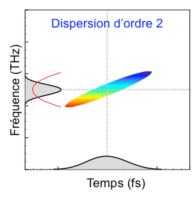


Figure A1.1: Spectrographs of an ideal pulse (left) and a pulse that has passed through a medium with normal dispersion [courtesy of Franck Morin, class of 2007].

#### Self-phase-modulation changes the time phase

Suppose a Gaussian pulse with the following expression:

$$I(t) = I_0 e^{-\frac{t^2}{2(\Delta \tau)^2}}$$

Therefore, when the pulse propagates in a medium with the Kerr effect, the intensity at one point in the medium will vary over time. This will cause a temporal variation in the index seen by the wave. The instantaneous phase acquired by the pulse as it passes through the medium of thickness L then depends on the time according to:

$$\phi(t) = \omega_0 t - \frac{2\pi}{\lambda_0} (n_0 + n_2 I(t)) L$$

The pulsation  $\omega = 2\pi v$  of the pulses, defined as the time derivative of the instantaneous phase, is therefore of the form :

$$\omega(t) = \omega_0 + \frac{2\pi n_2 L I_0}{\lambda_0 \Delta \tau^2} t e^{-\frac{t^2}{2(\Delta \tau)^2}}$$

So we can see that there is a temporal dependence of the pulsation. New frequencies are therefore created. There is a red shift in the leading edge of the pulse and a blue shift in the trailing edge (see Figure A1.2). In the case of self-phase-modulation, the frequency drift is positive. In addition, the temporal phase is modified. However, self-phase-modulation does not change the pulse duration.

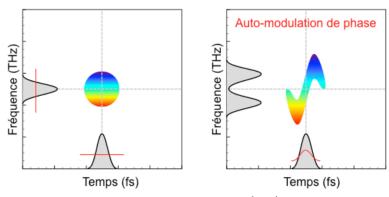


Figure A1.2: Spectrograms of an ideal pulse (left) and a pulse modified by self-phase-modulation (right) [courtesy of Franck Morin, class of 2007].

## 5.2 Appendix 2 - Solitonic Regime

The solitonic regime is the solution to Schrödinger's non-linear equation of writing the electric field envelope |a| of a pulse propagating in a dispersive, non-linear medium:

$$i\frac{\partial a}{\partial z} - \frac{\beta_2}{2}\frac{\partial^2 a}{\partial t^2} + \gamma |a|^2 a = 0$$

where  $\beta_2$  is the second order dispersion coefficient, corresponding to the group velocity dispersion. By doing Taylor development of the spectral phase around the central wavelength, we find:

$$\beta_2 = \frac{\lambda^3}{2\pi c^2} \frac{d^2 n}{d\lambda^2}$$

and the non-linear coefficient  $\gamma$  corresponding to self-phase-modulation. It is related to the non-linear Kerr index by :

$$\gamma = \frac{2n_2}{\lambda_0 w_0^2} \,.$$

It can be shown that it is necessary to have  $\gamma$  and  $\beta_2$  opposite signs for there to be a soliton type solution. This solution is written in the form of a hyperbolic square secant function.

$$P(t) = P_0 sech^2 \left(\frac{t}{1.76\Delta t}\right)$$

where  $\Delta t$  is the temporal width of the pulse at half height and  $P_0$  is the peak intracavity power.

In the case of the femtosecond laser oscillator in this labwork, self-phase-modulation and dispersion occur in different media and not simultaneously. However, since the variations due to these two phenomena at each round trip are small, the laser's pulse regime can be assimilated to the soliton regime. It is shown that there is then a relationship between the pulse duration at mid-height  $\Delta t$ ,  $\gamma$  and  $\beta_2$  (called the soliton area formula):

$$\Delta t = \frac{-\beta_2}{\gamma |a|^2} = \frac{-\phi_{2,cavit\acute{e}}}{\gamma L_{cristal} |a|^2}$$

With: 
$$\phi_{2,cavit\acute{e}} = \phi_{2,prismes} + \phi_{2,mat\acute{e}riau} + \phi_{2,miroir}$$

It is shown that for one pass in the Ti:sapphire crystal:

$$\phi_{2,mat\acute{e}riau} = \frac{\lambda_0^3}{2\pi c^2} \frac{\mathrm{d}^2 n}{\mathrm{d}\lambda^2} L_{cristal}$$

 $\phi_{2,\text{mirror}} \simeq 0$  (this quantity is neglected here)

$$\phi_{2,prismes} \simeq -\frac{2\lambda_0^3}{\pi c^2} \left(\frac{dn}{d\lambda}\right)^2 D + \frac{2\lambda_0^3}{2\pi c^2} \frac{d^2n}{d\lambda^2} e$$

where D is the distance (apex) between the two prism tips and e is the thickness of the crossed prism.

The first term of the equation on  $\phi_{2,prismes}$  is negative and allows to (over)compensate the dispersion of the sapphire crystal. The second term is positive and allows to finely adjust the total dispersion of the cavity: one of the prisms is positioned on a vernier in order to control e.

### 5.3 Appendix 3 - Calculation of extra-cavity dispersion

Let's define a pulse of width at 1/e in intensity  $t_{in}$  (note that  $2\sqrt{ln2}t_{in} = \Delta T_{FWHM}$ ).

We have:

$$E_{in}(t,0) = e^{-\frac{t^2}{2t_{in}^2}}$$

By doing the Fourier transform, we obtain:

$$E_{in}(\omega,0) = \sqrt{2\pi t_{in}^2} e^{-\frac{\omega^2 t_{in}^2}{2}}$$

After propagation over a length z in a material with a coefficient of dispersion  $\beta_2$ . The pulse accumulates a spectral phase, allowing us to deduce:

$$E(\omega, z) = \sqrt{2\pi t_{in}^2} e^{-\omega^2 \left(\frac{t_{in}^2}{2} - \frac{i\beta_2 z}{2}\right)}$$

An inverse Fourier transform is used to determine the equation of field evolution as a function of time. After propagation over a distance z, the field is written as:

$$E_{out}(t,z) = E_0 e^{-\frac{4ln2.t^2}{2\Delta t^2 + 8i.ln2.\beta_2 z}}$$

Thus  $\Delta t_{in}$  and the total mid-height  $\Delta t_{out}$  widths (FWHM) of the input and output pulses are related by the relation :

$$\Delta t_{out} = \Delta t_{in} \sqrt{1 + \left(\frac{4ln2. \beta_2 z}{\Delta t_{in}^2}\right)^2}$$

# 5.4 Appendix 4 - Photo of the laser cavity

For Laser alignment

Cavity end mirror

Accessible

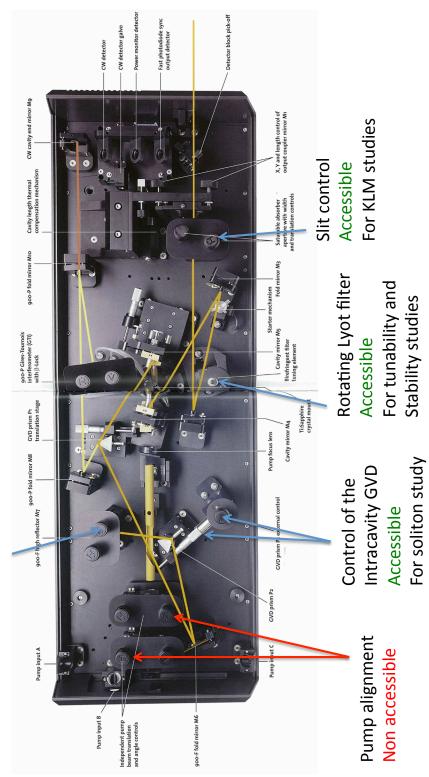


Figure A4.1: Coherent Mira 900 cavity